Exam	Seat	No: Enrollment No:	
		C.U.SHAH UNIVERSITY	
Subjec	t Cod	e :4SC02MTC1 Summer Examination-2014	Date: 26/05/2014
Subjec	t Nam	e: Mathematics - II	
Brancl Exami	1/Sen natioi	ester:- B.Sc(Science)/II 1: Regular	Time:02:00 To 5:00
Instru (1) Att (2) Use (3) Ins (4)Dra (5) Ass	ctions empt e of P tructions w near sume	s:- all Questions of both sections in same answer book / Supplementary rogrammable calculator & any other electronic instrument is prohibited. ons written on main answer Book are strictly to be obeyed. t diagrams & figures (If necessary) at right places suitable & Perfect data if needed	
		SECTION-I	
Q-1	a)	Find polar form of (i) $1 + i$ and (ii) $\sqrt{3} - i$.	(02)
	b)	Prove that $\cos h^2 x - \sinh^2 x = 1$.	(02)
	c)	Simplify: $\frac{(\cos 3\theta + i \sin 3\theta)^2 (\cos 4\theta - i \sin 4\theta)^{-2}}{(\cos 2\theta - i \sin 2\theta)^{-7}}$	(01)
	d)	Evaluate: $\int_0^{\pi/2} \cos^6 x dx$.	(01)
	e)	Define limit point of a sequence.	(01)
Q-2	a)	Find all fourth roots of unity and sketch them on unit circle.	(05)
	b)	Prove that $\cos 5\theta = 16 \cos^5 \theta - 20\cos^3 \theta + 5\cos \theta$.	(05)
	c)	Prove that $(1+i)^n + (1-i)^n = 2^{\frac{n}{2}+1} \cos \frac{n\pi}{4}$.	(04)
		OR	
Q-2	a)	State and prove De Moivre's theorem.	(05)
	b)	Prove that $\cos h^{-1}(z) = \log (z + \sqrt{z^2 - 1}).$	(05)
	c)	If $log(x + iy) = 2 - \frac{3\pi}{4}i$ then find value of x and y.	(04)
Q-3	a)	Prove that $\int \cos^n x dx = \frac{\cos^{n-1}x \sin x}{n} + \frac{n-1}{n} I_{n-2}$, for $\in N$.	(05)
	b)	Evaluate: $\int_{0}^{1/2} x^{3} (1 - 4x^{2})^{1/2} dx$	(05)
	c)	Using definition of limit prove that $\lim_{n\to\infty} x_n = \frac{2}{3}$, if $x_n = \frac{2n}{3n}$.	$\frac{+1}{+5}$ (04)
0.2	<i>a)</i>	Evaluate: $\int_{-\infty}^{\infty} \frac{x^2}{dr} dr$	(05)
Q-3	a)	$J_0 \frac{(1+x^6)^{7/2}}{(1+x^6)^{7/2}}$	(03)
	b)	Prove that $\int_0^1 x^m (1-x)^n dx = \frac{m(n)}{(m+n+1)!}$.	(05)
		Page 1 of 2	
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c)	Using definition	of limit prove that $\lim_{n\to\infty}$	$\sqrt[n]{n} = 1$	(04)
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SECTION-II

Q-4	a) Solve: $\frac{d^2y}{dx^2} + 5\frac{dy}{dx} + 6y = 0$	(02)
	b) Write condition that the plane $lx + my + nz = 0$ be a tangent to the	(02)
	cone $ax^2 + by^2 + cz^2 + 2fyz + 2gzx + 2hxy = 0$.	
	c) Write general equation of ellipsoid.	(01)
	d) Which is the vertex of cone having second degree homogeneous	(01)
	equation in x , yand z .	
	e) Find $\frac{1}{D^2} x^4$.	(01)
	a du	
Q-5	a) Solve: $(D^2 - 7D + 6)y = 2e^{3x}$, given that $y = 1, \frac{dy}{dx} = 0$ when $x = 0$.	(05)
	b) Solve: $y''' - 3y'' + 9y' - 27y = \cos 3x$	(05)
	c) Solve: $(D^2 - 4D + 1)y = e^{2x} \sin x$.	(04)
	OR	
Q-5	a) Solve: $(D^2 - 5D + 6)y = x + e^{4x}$ where $M^{1/2}$	(05)
	b) Solve: $\frac{dx}{dt} + y = \sin t$, $\frac{dy}{dt} + x = \cos t$	(05)
	c) Solve: $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 4y = 2x^2$.	(04)
Q-6	a) Find equation of cone whose vertex is the point $(1, 1, 0)$ and whose	(05)
	guiding curve is $x^2 + z^2 = 4$, $y = 0$.	
	b) Find equation of lines in which the plane $2x + y - z = 0$ cuts the	(05)
	colle $4x - y + 5z = 0$. c) Prove that equation of right circular cylinder whose axis is the line	(04)
	c) Frow that equation of right checkia cylinder whose axis is the line $x - \alpha = \frac{y - \beta}{z} = \frac{z - \gamma}{z}$ and radius <i>r</i> is	(04)
	$\frac{1}{n} = \frac{1}{m} = \frac{1}{n}$ and radius 7 is	
	$(x - \alpha)^2 + (y - \beta)^2 + (z - \gamma)^2$	
	$-\frac{[l(x-a) + m(y-b) + n(z-y)]}{l^2 + m^2 + m^2} = r^2$	
	$l^2 + m^2 + n^2$	
0-6	a) Check whether the equation $2x^2 + 2y^2 + 7z^2 - 10yz - 10yz + 2x$	Ŧ
Qυ	2y + 26z - 17 = 0 represent a cone with vertex at (2.2.1) or not.	(05)
	b) Find the equation of the cylinder whose generators are parallel to the	(05)
	line $\frac{x}{1} = \frac{y}{z^2} = \frac{z}{z}$ and whose guiding curve is $x^2 + 2y^2 = 1, z = 0$.	
	c) Prove that locus of lines through the vertex of cone $ax^2 + by^2 + cz^2$	+ (04)
	2fyz + 2gxz + 2hxy = 0 and perpendicular to it's tangent plane is	
	$Ax^{2} + By^{2} + Cz^{2} + 2Fyz + 2Gxz + 2Hxy = 0.$	
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Page 2 of 2

26